Multiverse Recursive Descent Grammar Exploration

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• Recursive Descent Parsing as a **case study** for Multiverse Debugging.



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- Recursive Descent Parsing as a **case study** for Multiverse Debugging.
- Helping me get out of my rabbit hole.



I would characterise my presentation today as follows:

- Recursive Descent Parsing as a **case study** for Multiverse Debugging.
- Helping me get out of my rabbit hole.
- A personal confirmation I still nurture a parsing bug.



A General Framework for Multiverse Debugging

Temporal Breakpoints for Multiverse Debugging

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Figure: DOI: https://doi.org/10.1145/3623476.3623526

Language-parameteric debugging framework for non-deterministic/concurrent executions.

 \hookrightarrow compare with *Stepwise debugging*: step through the execution of a program to observe evolution of state and effects, halting at selected 'breakpoints'

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record and revisit previous, selected execution points to observe state and effects

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Exploratory programming: build towards a larger program by attempting, comparing and revisiting alternative extensions

 \hookrightarrow *Omniscient/Back-in-time debugging*:

record and revisit previous, selected execution points to observe state and effects

 \hookrightarrow *Multiverse debugging*: (exhaustive) exploration of concurrent executions (with state reductions and temporal breakpoints)

Interactive programming models

Commonality

A transition relation state \xrightarrow{action} state' describes a tree of executions and reachable states.

A Principled Approach to REPL Interpreters

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Question: In what ways can an omniscient, exploratory, multiverse debugger for grammars assist the grammar engineering process?

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Similarly: A complete, generalised parser attempts to find all executions that generate a particular sentence (the input sentence of the parser).

Question: In what ways can an omniscient, exploratory, multiverse debugger for grammars assist the grammar engineering process?

Today

- A theoretical **framework** for multiverse grammar exploration based on the execution threads encountered in recursive-descent parsers
- A prototype implementation of a **tool** that supports sentence generation, deterministic parsing, error-recovery, deterministic error diagnosis, ...
- TODO: error diagnosis in complete parsing, evaluation: does anyone want this?

A grammar G is a set of productions of the form (X, α) with:

- $X \in N$, referred to as the left-hand side, with N the set of nonterminals
- $\alpha \in (\mathsf{N} \cup \mathsf{T})^*$, referred to as the right-hand side
- $T \cap N = \emptyset$, with T the set of terminals

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Definition

The relations $\alpha \rightarrow \beta$ (derivation steps) and $\alpha \rightarrow \tau$ (left-most derivations) are defined as the smallest set such that:

- $X \to \alpha$ if and only if $(X, \alpha) \in G$
- $\tau X \alpha \rightarrow \tau \beta \alpha$ if and only if $X \rightarrow \beta$ and $\tau \in T(G)^*$ (the terminal symbols occuring in G)
- $\alpha_0 \dashrightarrow \tau$ if and only if there is a sequence $\alpha_0 \to \alpha_1$, $\alpha_1 \to \alpha_2$, ..., $\alpha_{n-1} \to \tau$ with $n \ge 0$

The language L(G) described by grammar G is the set of all sentences τ with $\mathcal{X} \dashrightarrow \tau$ (and $\mathcal{X} \in N$ a nominated start nonterminal).

$$\mathcal{X} \to A; \mid B$$

 $A \to a A \mid \epsilon$
 $B \to B b \mid \epsilon$

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- -

	$\mathcal{X} ightarrow A;$
$\mathcal{X} o A$; $\mid ~B$	ightarrow aA;
$A ightarrow a \ A \ \mid \ \epsilon$	ightarrow aaA;
$B ightarrow B \ b \ \mid \ \epsilon$	ightarrow aaa A ;
	\rightarrow 222.

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Recursive-Descent Parsing: choose alternates based on next token expectation from input

$$\begin{array}{l} \mathcal{X} \to A \ ; \ | \ B \\ A \to a \ A \ | \ \epsilon \\ B \to B \ b \ | \ \epsilon \end{array}$$

Input: [] [b ,b]
Next action:descend(X, B)

Stack: [($\mathcal{X}' \rightarrow \cdot \mathcal{X}, 0$)]

$$\mathcal{X} \to A; \mid B$$

 $A \to a A \mid \epsilon$
 $B \to B b \mid \epsilon$

Input: [] [b ,b] Next action: **descend**(*B*, *Bb*)

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$\mathcal{X} o A$; B $A o a A$ ϵ	Input: [b][b] Next action:	ascend
$B ightarrow B \ b \ \mid \ \epsilon$		

.

Stack: [$(\mathcal{X}' \to \cdot \mathcal{X}, 0)$, $(\mathcal{X} \to \cdot B, 0)$, $(B \to \cdot Bb, 0)$, $(B \to Bb \cdot, 0)$]

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$$\mathcal{X} \to A$$
; | B
 $A \to a A$ | ϵ
 $B \to B b$ | ϵ

Input: [b, b] [] Next action: ascend

Stack: [($\mathcal{X}'
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$$\mathcal{X} \to A; \mid B$$

 $A \to a A \mid \epsilon$
 $B \to B b \mid \epsilon$

Input: [b, b][] Next action: accept

Stack: [($\mathcal{X}' \to \mathcal{X} \cdot, 0$)]

 $\mathcal{X} \to A; \mid B$ $A \to a A \mid \epsilon$ $B \to B b \mid \epsilon$ Input: [b, b][] Next action: accept

Stack: [$(\mathcal{X}' o \mathcal{X} \cdot, 0)$]

Common problems in RD-Parsing

- Left-recursion: choosing the same alternative without progress
- Non-predictive: alternates have (indirect) common prefixes
- Non-determinism cannot be avoid in general case (without solving the parse problem)

Syntax Analysis – Alternative

Definition – Syntax of Actions

```
a: action ::= match(t) | descend(X, \alpha) | ascend | accept
Constraints: t \in T, X \in N, \alpha \in (T \cup N)^*
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Definition – Semantics of Actions

A configuration γ is a structure $\langle S, i \rangle$ with:

- S a call-stack; a sequence of *items* denoted $[(X \rightarrow \alpha \cdot \beta, k), S']$ with $k \ge 0$
- $i \ge 0$ an index into some input sentence \mathcal{I} .

The semantics of actions is captured by the transition relation $\gamma \xrightarrow{a} \gamma'$.

A (complete) parsing *thread* is a (longest) sequence $\langle [(\mathcal{X}' \to \mathcal{X}, 0)], 0 \rangle \xrightarrow{a_0} \dots \xrightarrow{a_n} \langle S, m \rangle$ (for some *m* and $\mathcal{X}' \in N, \mathcal{X}' \notin N(G)$). A thread is successful if S = [].

Evolution of RDP Programs in transition system Γ_S

$$\frac{l_{i} = t \quad s = t}{\langle [(X \to \alpha \cdot s\beta, k), S], i \rangle \xrightarrow{match(t)} \langle [(X \to \alpha t \cdot \beta, k), S], i + 1 \rangle} \text{MATCH}} \\
\frac{s = X \quad (X, \delta) \in G}{\langle [(Y \to \alpha \cdot s\beta, k), S], i \rangle \xrightarrow{descend(X, \delta)} \langle [(X \to \cdot \delta, i), (Y \to \alpha \cdot X\beta, k), S], i \rangle} \text{DESCEND}} \\
\frac{[(Y \to \alpha \cdot x\beta, k'), S'] = S}{\langle [(X \to \alpha \cdot, k), S], i \rangle \xrightarrow{ascend} \langle [(Y \to \alpha X \cdot \beta, k'), S'], i \rangle} \text{ASCEND}} \\
\frac{|\mathcal{I}| = i}{\langle [(\mathcal{X}' \to \mathcal{X}, 0)], i \rangle \xrightarrow{accept} \langle [], i \rangle} \text{ACCEPT}}$$

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Evolution of RDP Programs in transition system Γ_G

$$\frac{s = t}{\langle [(X \to \alpha \cdot s\beta, k), S], i \rangle \xrightarrow{match(t)} \langle [(X \to \alpha t \cdot \beta, k), S], i + 1 \rangle} \text{MATCH}} \\
\frac{s = X \quad (X, \delta) \in G}{\langle [(Y \to \alpha \cdot s\beta, k), S], i \rangle \xrightarrow{descend(X, \delta)} \langle [(X \to \cdot \delta, i), (Y \to \alpha \cdot X\beta, k), S], i \rangle} \text{DESCEND}} \\
\frac{[(Y \to \alpha \cdot x\beta, k'), S'] = S}{\langle [(X \to \alpha \cdot, k), S], i \rangle \xrightarrow{ascend} \langle [(Y \to \alpha X \cdot \beta, k'), S'], i \rangle} \text{ASCEND}} \\
\frac{\overline{\langle [(X' \to X, 0)], i \rangle \xrightarrow{ascept}} \langle [], i \rangle} \text{ACCEPT}}{\langle \overline{\langle [(X' \to X, 0)], i \rangle \xrightarrow{accept}} \langle [], i \rangle}}$$

Demo 1 – guided sentence generation

For every **parse tree** of \mathcal{I} there is exactly one successful thread in Γ_S and vice versa.

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A general parser does the above for any context-free grammars (no restrictions).

Common solutions to problems with RD-Parsing

Recall: Common problems in RD-Parsing

- Left-recursion: choosing the same alternative without progress
- Non-predictive: alternates have (indirect) common prefixes
- Non-determinism cannot be avoid in general case (without solving the parse problem)

Common solutions to pruning undesirable paths

- Left-recursion removal: preserves language, modifies set of threads
- Alternative: make at most $\mid \mathcal{I} \mid$ recursive calls
- Left-factoring: preserves language, modifies set of threads
- *k*-lookahead: sound, reduces set of threads
- Accepting only predictive, LL(k)-grammars: not general

Defining – Language-Preserving Pruning Strategies

A pruning strategy defines additional conditions (on top of Γ_G), removing transitions $\gamma \xrightarrow{a} \gamma'$.

A pruning strategy is *language preserving* if it reduces the set of threads whilst preserving, for every sentence in the language, <u>at least one</u> successful thread yielding that sentence.

A pruning strategy is *sound* if it reduces the set of threads without removing successful threads.

Note: left-biased choice not language-preserving, lookahead is.

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Definition – Ambiguity Reduction Strategies

A *perfect disambiguation strategy* is a language-preserving pruning strategy that preserves exactly one successful thread for every sentence in the language.

Note: many practical disambiguation strategies are not perfect (e.g., follow-restriction)

Pruning Examples

Definition – one token lookahead pruning

Remove $\langle S, k \rangle \xrightarrow{\operatorname{descend}(X,\alpha)} \gamma'$ for any S, k, γ', X, α if it holds that every shortest sub-thread $\gamma' \xrightarrow{a_1} \ldots \xrightarrow{a_n} \gamma_n$ that ends with

•
$$a_n = \operatorname{match}(t)$$
 has $t \neq \mathcal{I}_k$, or

•
$$\gamma_n = \langle [(\mathcal{X}' \to \mathcal{X} \cdot, 0)], k' \rangle$$
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 has $k' \neq |\mathcal{I}|$.

Definition – left-recursion termination

Remove $\langle S, k \rangle \xrightarrow{\text{descend}(X,\alpha)} \gamma'$ for any S, k, γ', X, α when S has $|\mathcal{I}|$ or more items of the form $(Y \to \ldots, X, \ldots, k)$ for any Y.

i.e., $|\mathcal{I}|$ descend actions have already been performed on X without progress. Note: this pruning strategy is unsound for some grammars.

Definition -k-actions lookahead

Remove $\gamma_0 \xrightarrow{\operatorname{descend}(X,\alpha)} \gamma_1$ if all (subsequent) threads of k actions or less cannot transition (considering any collection of additional pruning strategies).

With this strategy, a descend action is only possible if all subsequent threads are of a length i > k or at least one successful thread has been identified.

Demo 2 with the different pruning strategies applied.

Deterministic parse error diagnosis

The parse error diagnosis problem:

Given a stack-trace and an input sentence location, answer the following: Did I expect to be at a different grammar location or a different input sentence location? Does the grammar or input require modification?

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Suggested protocol for using RDP-Debugging tool:

- 1. Configure tool to use same lookahead strategy as employed parser
- 2. Run on grammar and input until parse error.
- 3. Observe stack-trace and input location.
- 4. Weaken input sentence constraints (move from Γ_S to Γ_G semantics).
- 5. Experiment with additional or dropped tokens (error recovery, next slide).
- 6. Jump back to last transition that still matched expectation (omniscient debugging).
- 7. Weaken the applied set of lookahead/pruning strategies.
- 8. Explore alternative paths to better understand divergence from expectation.

Definition – Additional Syntax of Actions

Additional Rules for a System Γ_{err}

$$\frac{s = t}{\langle [(X \to \alpha \cdot s\beta, k), S], i \rangle \xrightarrow{match(t)} \langle [(X \to \alpha t \cdot \beta, k), S], i \rangle} \text{MATCH-ANY}}$$
$$\overline{\langle S, i \rangle \xrightarrow{drop} \langle S, i + 1 \rangle} \text{DROP}$$

Observation: Deterministic parsing is akin to finding *any* state which errors or accepts (assuming lookahead is sufficient to cancel all non-determinism).

Observation: Non-deterministic parsing akin to finding *all* states that error or accept.

Problem: due to non-determinism and ambiguity, parser can find many error threads! (possibly infinitely or exponentially many)

Question: how can multiverse debugging be used for diagnosing errors in complete parsing?

Conclusion

Where I am today

- A theoretical **framework** for multiverse grammar exploration based on the execution threads encountered in recursive-descent parsers
- A prototype implementation of a **tool** that supports sentence generation, deterministic parsing, error-recovery, deterministic error diagnosis, ...
- The underlying reachability graph can be modified on the fly by the user
- TODO: error diagnosis in complete parsing, evaluation: does anyone want this?

Case study conclusions

- Pruning strategies can be applied in other case studies to reduce search space
- Not all actions available to the user should be available to the breakpoint finder
- We'd like to have a find all <breakpoint> command (for non-deterministic parsing)

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